

科目名稱: 微積分 (下)(3學分)  
 考試時間: 3 月 13 日第二節  
 \* (每題 7 分, 滿分 105 分)

1. Calculate  $\int \tan x \, dx$ .
2. Use the logarithmic differentiation to find the derivative of the function  $y = \sqrt{\frac{x-1}{x^4+1}}$ .
3. Calculate  $\int_e^6 \frac{1}{x \ln x} \, dx$ .
4. Differentiate the function  $y = \ln |2 - x - 5x^2|$ .
5. Find  $y'$  if  $y = e^{-4x} \sin 5x$ .
6. Evaluate the integral  $\int_1^2 \frac{e^{\frac{1}{x}}}{x^2} \, dx$ .
7. Calculate  $\int_0^1 (x^e + e^x) \, dx$ .
8. Find  $y'$  if  $e^{\frac{x}{y}} = x - y$  and  $y$  is differentiable function of  $x$ .
9. Differentiate  $y = x^{\sqrt{x}}$ .
10. Calculate  $\int \frac{\log_{10} x}{x} \, dx$ .
11. Calculate  $\int 3^{\sin x} \cos x \, dx$ .
12. Find  $\lim_{x \rightarrow 0} \frac{\tan x - x}{x^3}$ .
13. Compute  $\lim_{x \rightarrow 0^+} \sin x \ln x$ .
14. Compute  $\lim_{x \rightarrow 0^+} x^{\sqrt{x}}$ .
15. Compute  $\lim_{x \rightarrow \frac{\pi}{2}^-} (\sec x - \tan x)$ .

| 題號 | 答案  | 來源           |
|----|---|--------------|
| 1  | $\ln  \sec x  + C$  | 6.2* - 例題 13 |
| 2  | $y' = \sqrt{\frac{x-1}{x^4+1}} \left( \frac{1}{2(x-1)} - \frac{4x^3}{2(x^4+1)} \right)$ | 6.2* - 習題 63 |
| 3  | $\ln(\ln 6)$  | 6.2* - 習題 70 |
| 4  | $\frac{-1-10x}{2-x-5x^2}$   | 6.2* - 習題 33 |
| 5  | $y' = -4e^{-4x} \sin 5x + 5e^{-4x} \cos 5x$   | 6.3* - 例題 5  |
| 6  | $e - e^{\frac{1}{2}}$   | 6.3* - 習題 93 |
| 7  | $\frac{1}{e+1} + e - 1$   | 6.3* - 習題 83 |
| 8  | $y' = \frac{y^2 - ye^{\frac{x}{y}}}{y^2 - xe^{\frac{x}{y}}}$                            | 6.3* - 習題 55 |
| 9  | $x^{\sqrt{x}} \left( \frac{1}{2\sqrt{x}} \ln x + \frac{1}{\sqrt{x}} \right)$            | 6.4* - 例題 4  |
| 10 | $\frac{1}{\ln 10} \frac{(\ln x)^2}{2} + C$  | 6.4* - 習題 47 |
| 11 | $\frac{3^{\sin x}}{\ln 3} + C$  | 6.4* - 習題 49 |
| 12 | $\frac{1}{3}$   | 6.8 - 例題 4   |
| 13 | 0   | 6.8 - 習題 44  |
| 14 | 1   | 6.8 - 習題 57  |
| 15 | 0   | 6.8 - 例題 8   |

\* 為非勾選習題、類似題。  
證明題、圖形題略過。